

# Caustics

Graphics?

USING PHOTON MAPS

CS500 RAY TRACING  
BORJA PORTUGAL MARTIN

# Caustics using Photon maps

## Contents

- ▶ Motivation
- ▶ Approach
- ▶ Photon maps
  - ▶ What are they used for?
  - ▶ What are they?
  - ▶ How are they generated?
    - ▶ Photon emission
      - ▶ Multiple lights
    - ▶ Photon tracing
      - ▶ Russian roulette
    - ▶ Photon storing
      - ▶ The photon
      - ▶ KD-Tree
      - ▶ Three maps
  - ▶ Summary
- ▶ Rendering
  - ▶ KD-Tree traversal
  - ▶ Sphere VS Disk
  - ▶ Radiance estimate
    - ▶ Formula
    - ▶ Filtering
  - ▶ Summary
  - ▶ Conclusion
    - ▶ Why photon mapping?
  - ▶ Credits

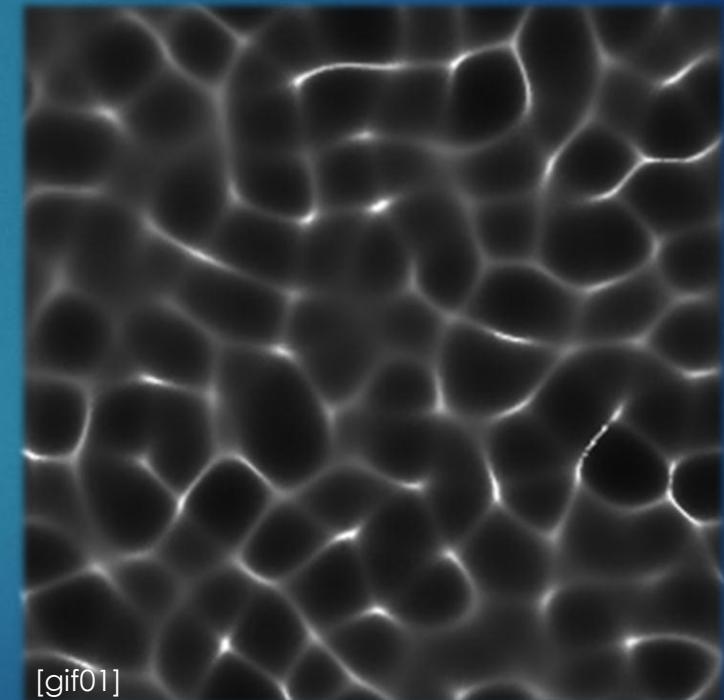
# Motivation



# Motivation

## Caustics in Video Games

- ▶ Real time applications fake caustics



# Motivation

## Ray traced caustics

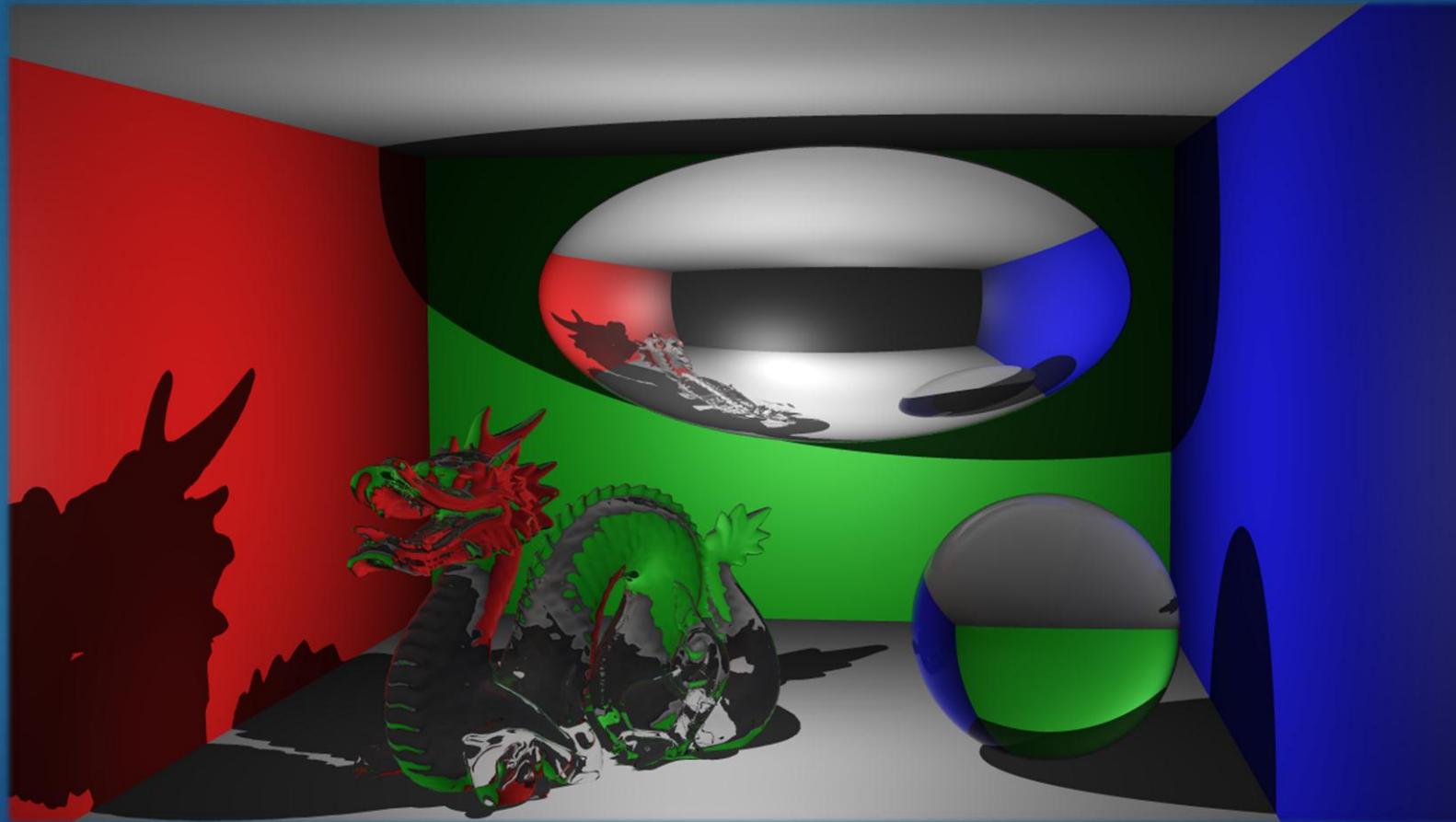
- Ray tracing is done offline, we can use all the computational power



# Caustics

## Motivation

- ▶ Glass in ray traced images without caustics do not seem correct



# Approach



# Approach

How can we do it?

- ▶ We want to simulate what light does
  - ▶ Cast rays from the light source until we reach the camera (too expensive)
- ▶ Possible approaches:
  - ▶ Monte Carlo integration
  - ▶ Photon mapping: similar, but faster, approach to Monte Carlo

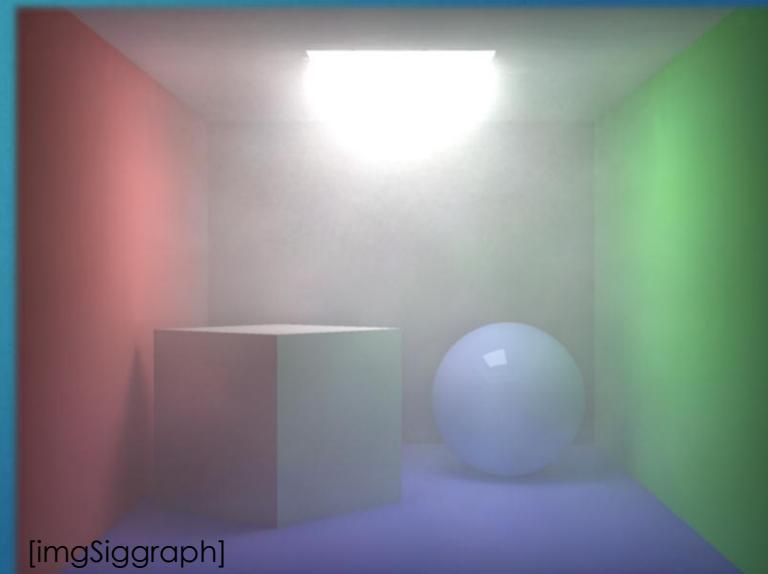
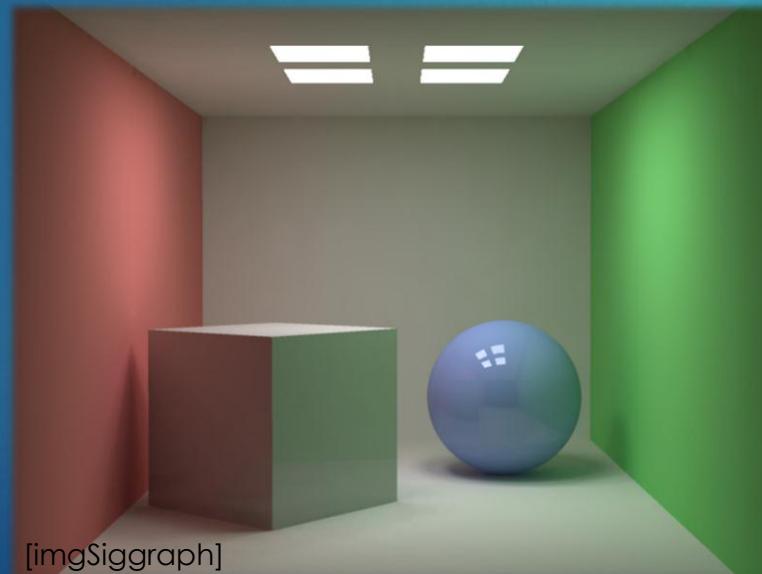
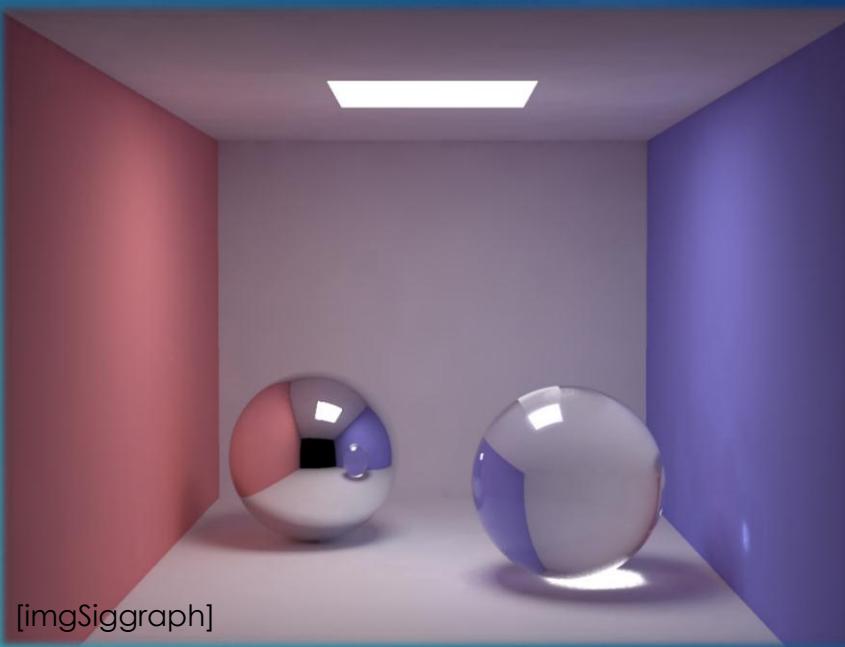
# Photon maps



# Photon maps

What are they used for?

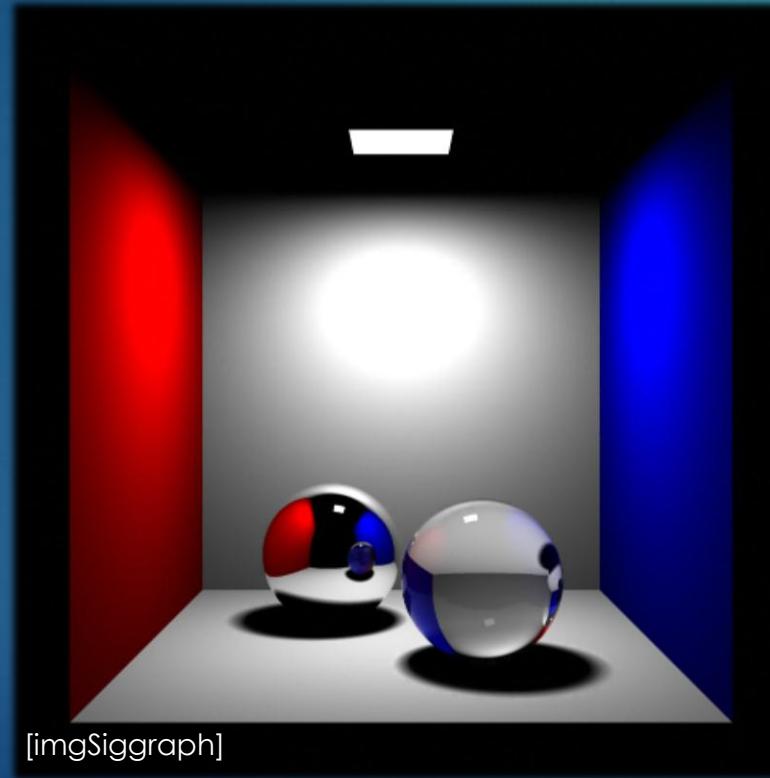
- ▶ Caustics
- ▶ Global illumination
- ▶ Participating media



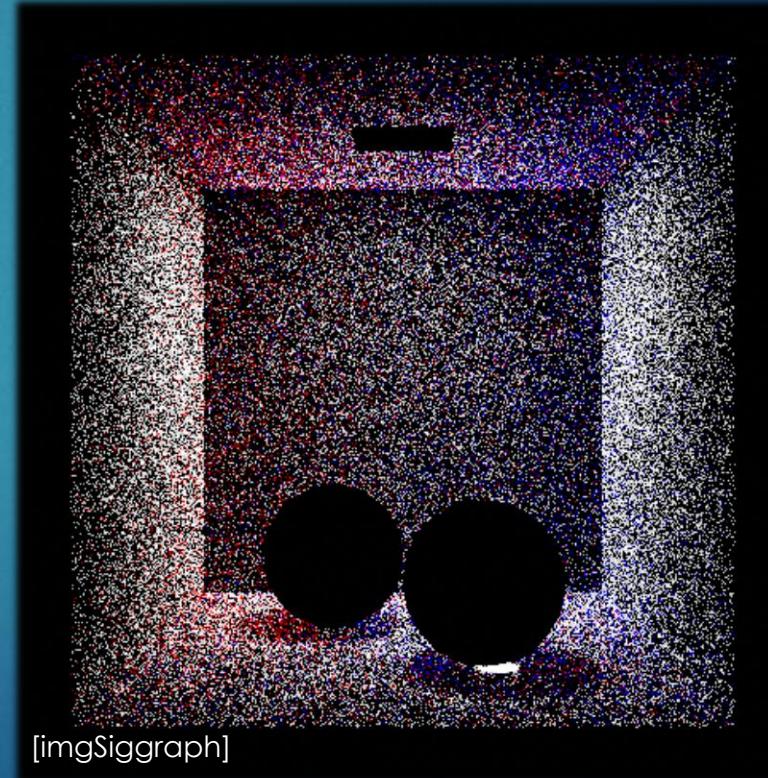
# Photon maps

What are they?

- ▶ Collection of photons (light rays that reached a diffuse surface)
- ▶ 3D (its name made me, at first, think they were 2D)



[imgSiggraph]



[imgSiggraph]

# Photon maps

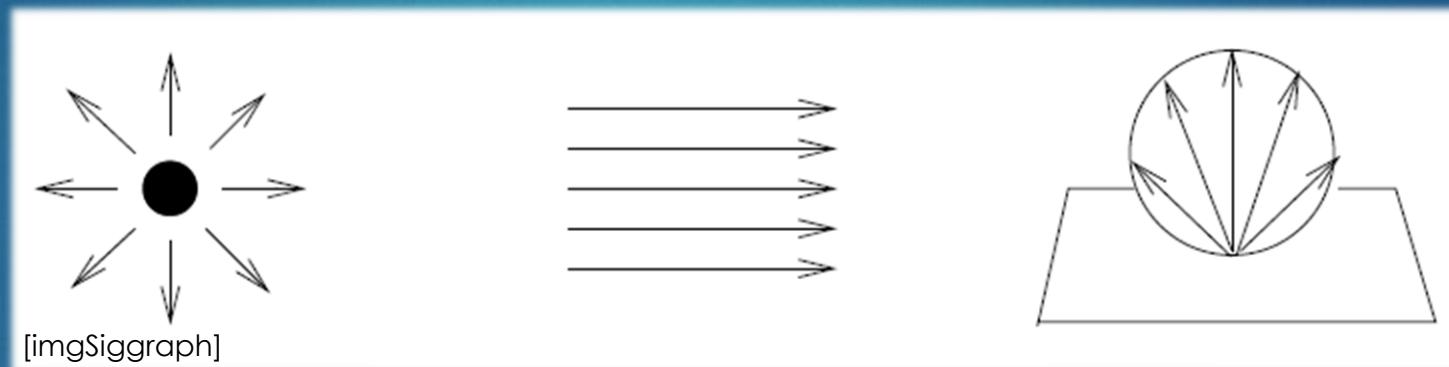
How are they generated?

1. Emit photons from the light sources
2. Trace photons until they reach a diffuse surface
3. Store them in a KD-Tree for fast access

# Photon maps

## Photon emission

- ▶ Photons are emitted from each light source
- ▶ Direction depends on the light type
  - ▶ Emission directions for point light, directional light and area light respectively



# Photon maps

## Photon emission

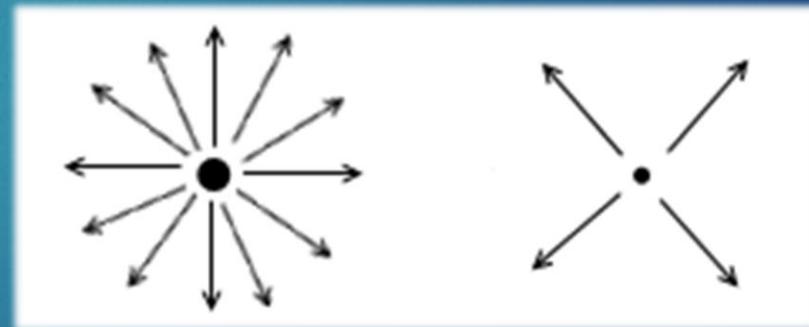
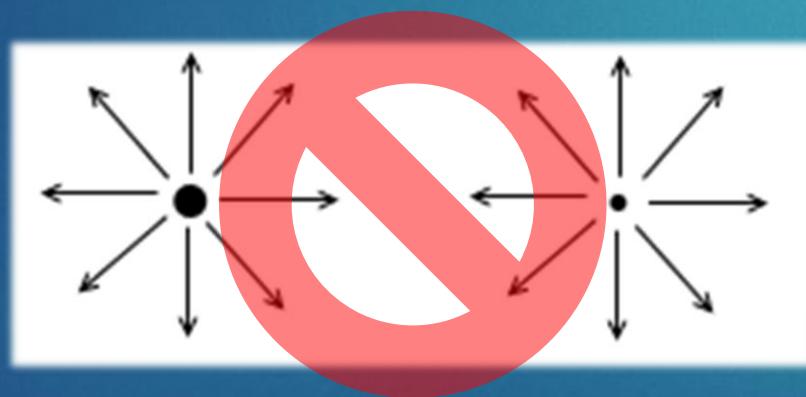
- ▶ Power of the photon
  - ▶ Information about the light source that emitted it
- ▶ Formula:
  - ▶  $P_{photon}$  Power of each photon
  - ▶  $P_{light}$  Power of the light
  - ▶  $n_e$  Number of photons the light will emit

$$P_{photon} = \frac{P_{light}}{n_e}$$

# Photon maps

## Photon emission – Multiple lights

- ▶ We don't emit the same number of photons per light
- ▶ Lights with more intensity will emit more photons
  - ▶ Number of photons in the scene remains constant
  - ▶ Photons will have similar power
    - ▶ Makes the radiance estimate better



# Photon maps

Photon emission – Multiple lights

	<b>Light A</b>	<b>Light B</b>	<b>Total</b>
Power	9	1	10
Contribution	90%	10%	100%
Number of photons	100	100	200
Photon power	$9/100 = 0.09$	$1/100 = 0.01$	10

	<b>Light A</b>	<b>Light B</b>	<b>Total</b>
Power	9	1	10
Contribution	90%	10%	100%
Number of photons	90	10	100
Photon power	$9/90 = 0.1$	$1/10 = 0.1$	10

# Photon maps

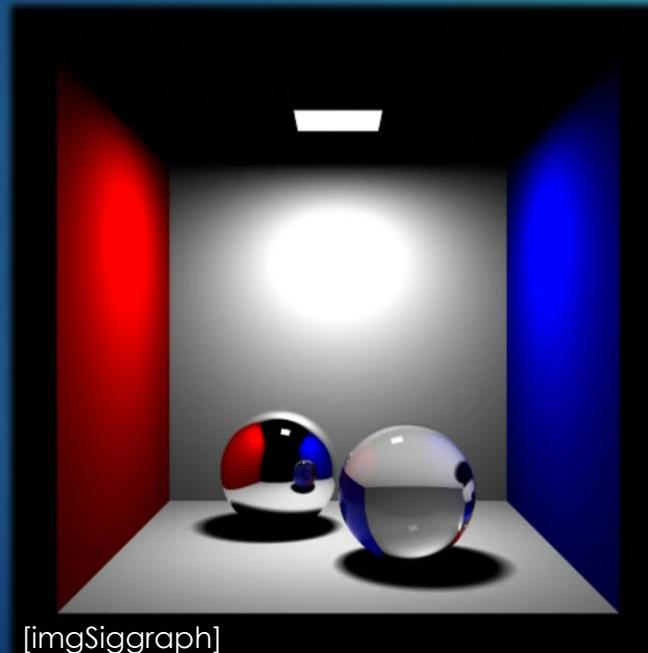
## Photon tracing

- ▶ Each time we hit a surface we would need to generate 2 photons
  - ▶ Diffuse reflection
  - ▶ Specular reflection
- ▶ The 8<sup>th</sup> bounce would generate  $2^8 = 256$  photons (this is bad)
  - ▶ A lot of memory needed
  - ▶ Most photons will have very low power
- ▶ Solution: Russian roulette
  - ▶ Probabilistic approach

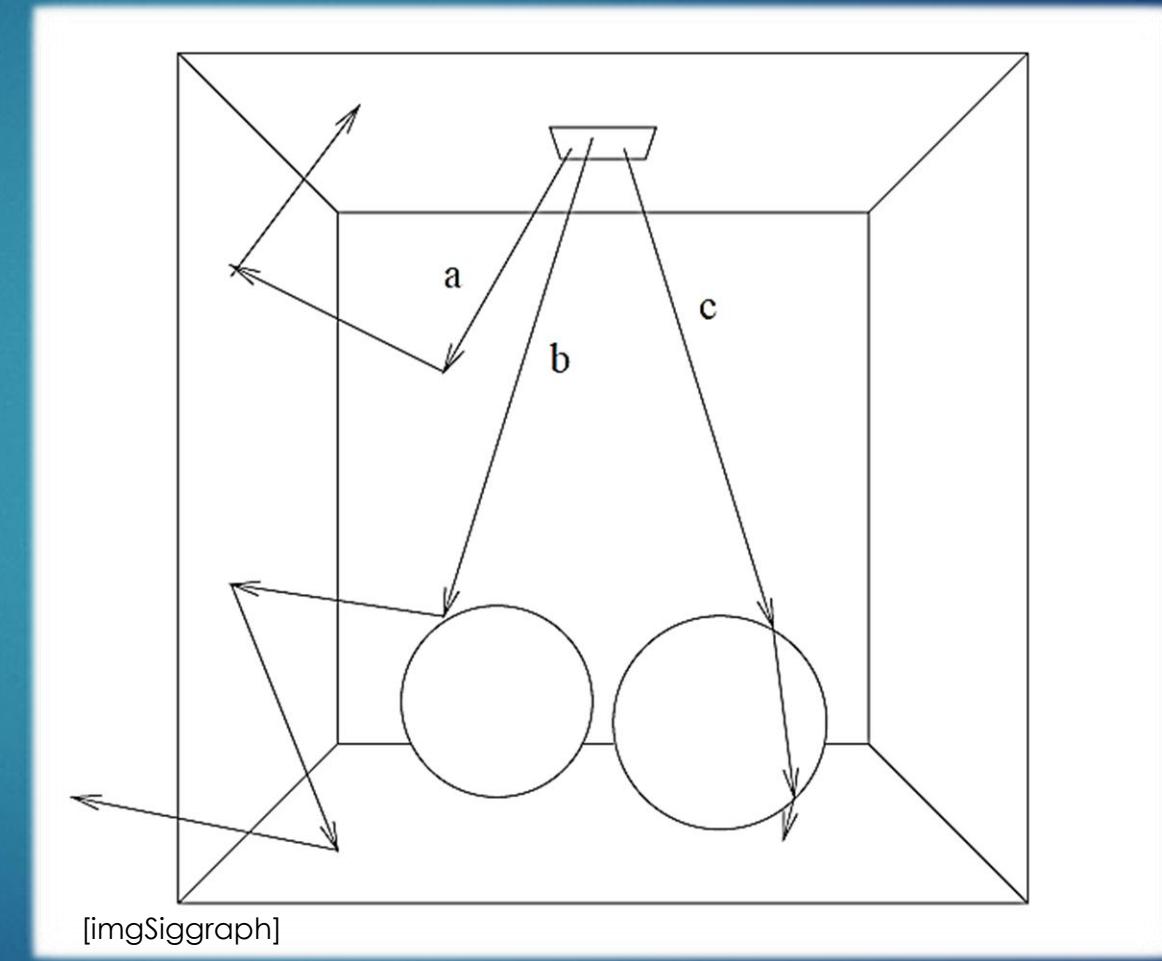
# Photon maps

## Photon tracing – Russian roulette

- ▶ Photon path examples:
  - ▶ a: x2 diffuse -> absorption
  - ▶ b: specular -> x2 diffuse
  - ▶ c: x2 specular -> absorption



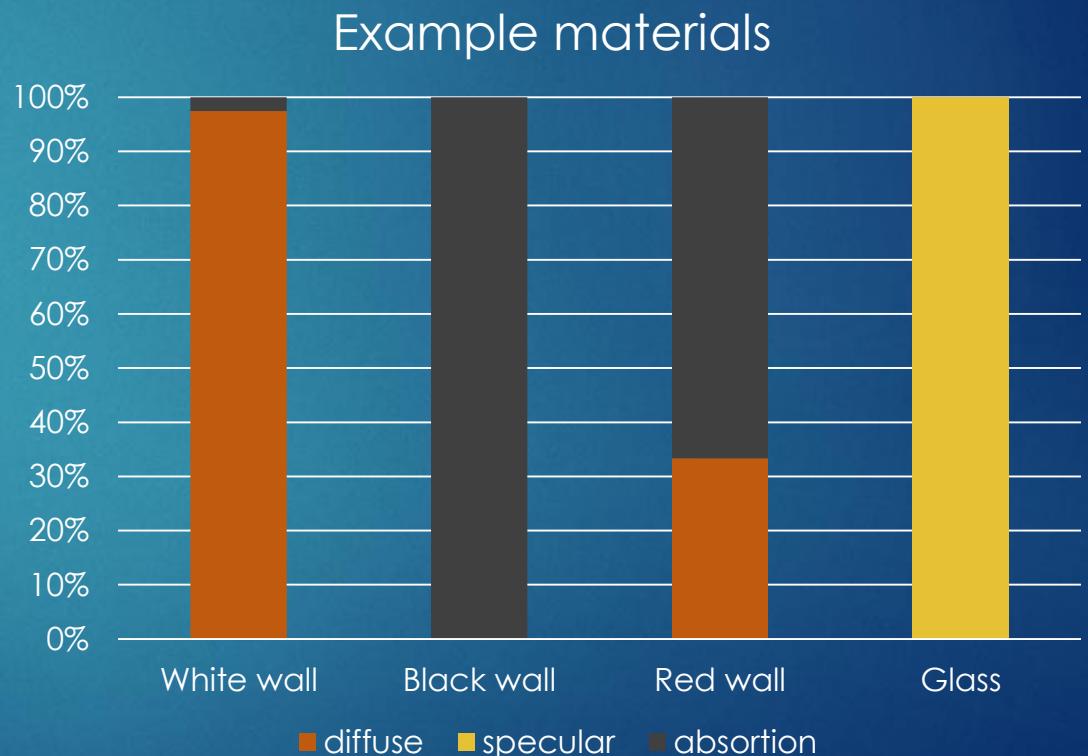
[imgSiggraph]



# Photon maps

## Photon tracing – Russian roulette

- ▶ Coefficients to determine the action of the photon
  - ▶  $D$  Diffuse reflection coefficient
  - ▶  $S$  Specular reflection coefficient
  - ▶  $D \geq 0, S \geq 0, D + S \leq 1$
- ▶ Take random  $x$  where  $x \in [0, 1]$ 
  - ▶  $x \in [0, D] \rightarrow \text{diffuse reflection}$
  - ▶  $x \in (D, D + S] \rightarrow \text{specular reflection}$
  - ▶  $x \in (D + S, 1] \rightarrow \text{absortion}$



# Photon maps

Photon tracing – Russian roulette

- ▶ Compute coefficients out of RGB coefficients

$$P_r = \max(d_r + s_r, d_g + s_g, d_b + s_b)$$

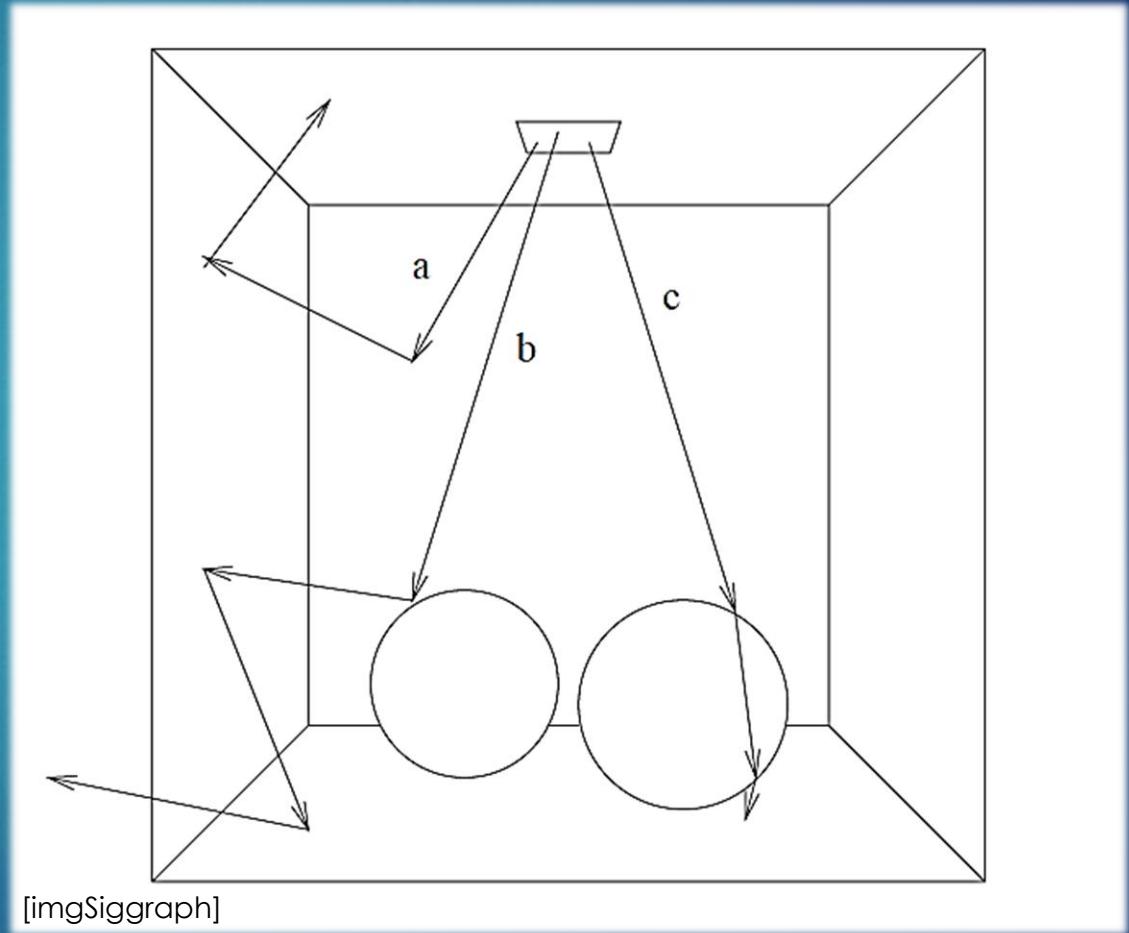
$$P_D = \frac{d_r + d_g + d_b}{d_r + d_g + d_b + s_r + s_g + s_b} P_r$$

$$P_S = \frac{s_r + s_g + s_b}{d_r + d_g + d_b + s_r + s_g + s_b} P_r = P_r - P_D$$

# Photon maps

## Photon tracing – Russian roulette

- ▶ Applying  $P_D$  and  $P_S$ 
  - ▶  $x \in [0, P_D] \rightarrow$  diffuse reflection
  - ▶  $x \in (P_D, P_D + P_S] \rightarrow$  *specular reflection*
  - ▶  $x \in (P_D + P_S, 1] \rightarrow$  *absortion*



# Photon maps

## Photon tracing – Russian roulette (Summary)

- ▶ Pros:
  - ▶ Reduces number of photon emission
    - ▶ Less computation & storage required
  - ▶ Keeps photon powers similar → Better radiance estimate
- ▶ Cons:
  - ▶ Increases variance on the solution, we need to emit a lot of photons
  - ▶ Not as many as without using Russian roulette

# Photon maps

## Photon tracing

- When a photon hits a surface we need to update its power

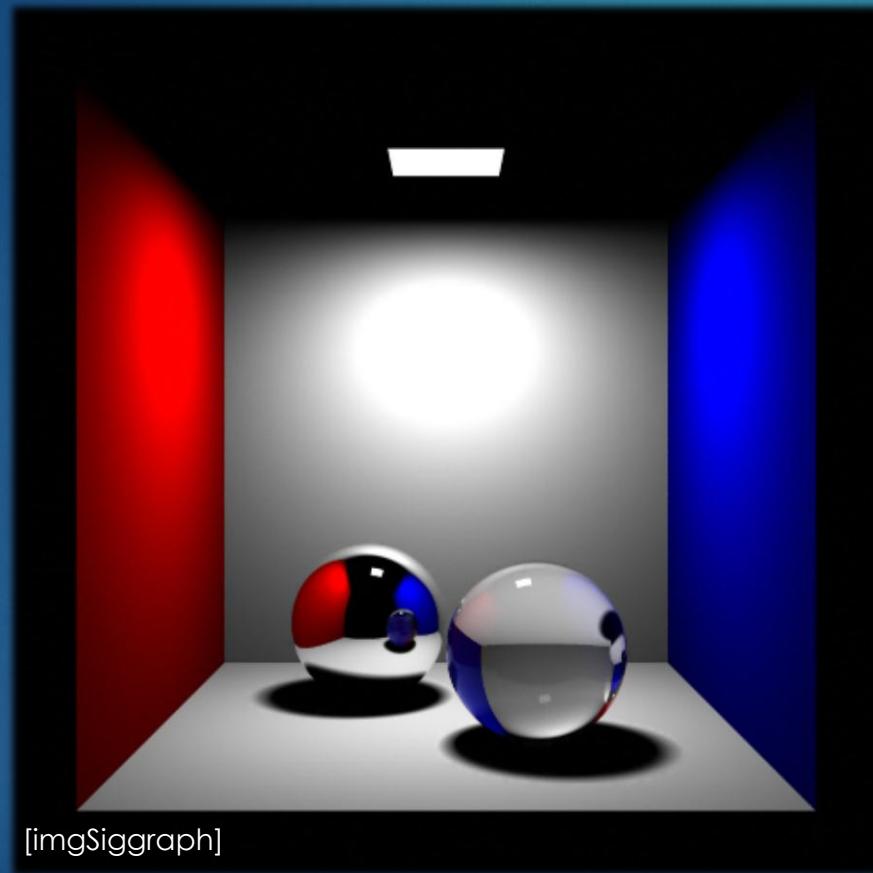
- $P_{inc}$  Power of the incident photon
- $P_{refl}$  Power of the reflected photon
- $S$  Specular color of the surface (if specular reflection happens)

$$P_{refl} = \frac{P_{inc} S}{P_S}$$

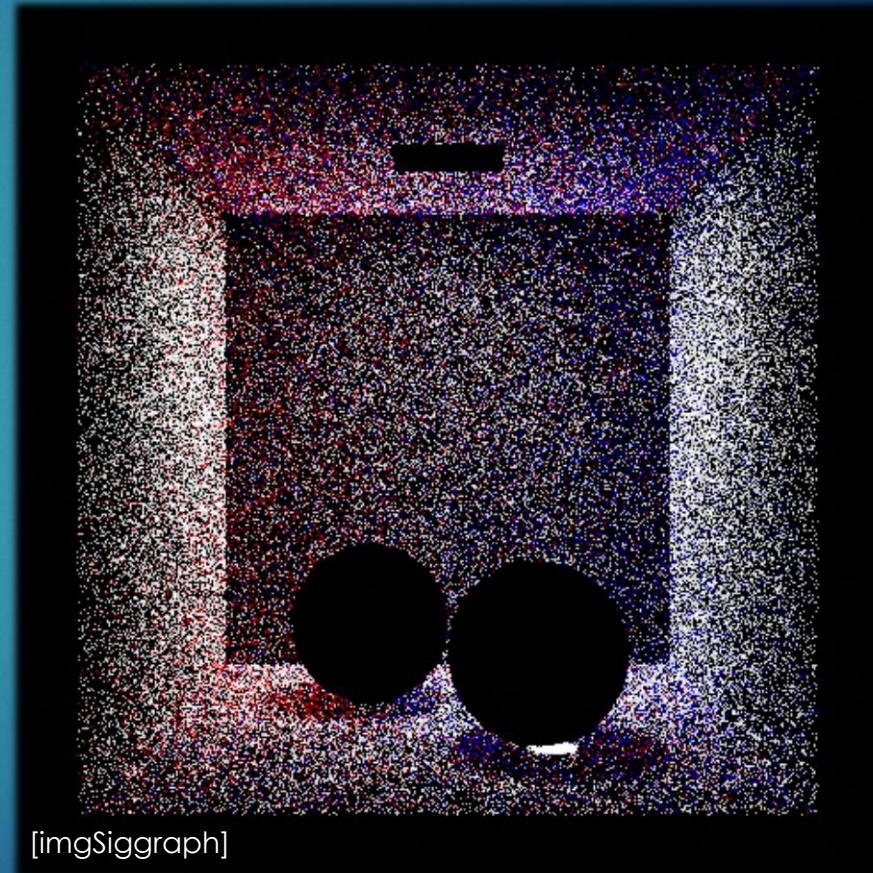


# Photon maps

Photon tracing



[imgSiggraph]



[imgSiggraph]

# Photon maps

Photon storing – The photon

```
struct photon
{
    float x, y, z;          // position
    float r, g, b;          // power
    float dx, dy, dz;        // incident direction
};    // 36 bytes
```

# Photon maps

Photon storing – The photon

- ▶ In case memory is a concern, compressed version

```
struct photon
{
    float x, y, z;    // position
    char p[4];         // power packed as 4 chars (Ward's RGBE)
    char phi, theta;  // compressed incident direction
                      // (spherical coordinates)
    short flag;        // flag used in kd-tree
};    // 20 bytes
```

# Photon maps

## Photon storing – The photon

- ▶ Ward's RGBE packing
  - ▶ Same principle of mantissa and exponent in floating point values
  - ▶ Normalize RGB floats to chars, exponent gives us more precision
    - ▶  $\text{RGB} \rightarrow [0, 255]$  red, green, blue values
    - ▶  $E \rightarrow [0, 255]$  Exponent

# Photon maps

Photon storing – The photon

- ▶ Incident direction packing
  - ▶  $2 \text{ chars} \rightarrow 16 \text{ bits} \rightarrow 2^{16} = 65536 \text{ possible directions}$

$$phi = 255 * \frac{atan2(dy, dx) + \pi}{2\pi}$$

$$[-\pi, \pi] \rightarrow [0, 2\pi] \rightarrow [0, 1] \rightarrow [0, 255]$$

$$theta = 255 * \frac{acos(dx)}{\pi}$$

$$[0, \pi] \rightarrow [0, 1] \rightarrow [0, 255]$$

# Photon maps

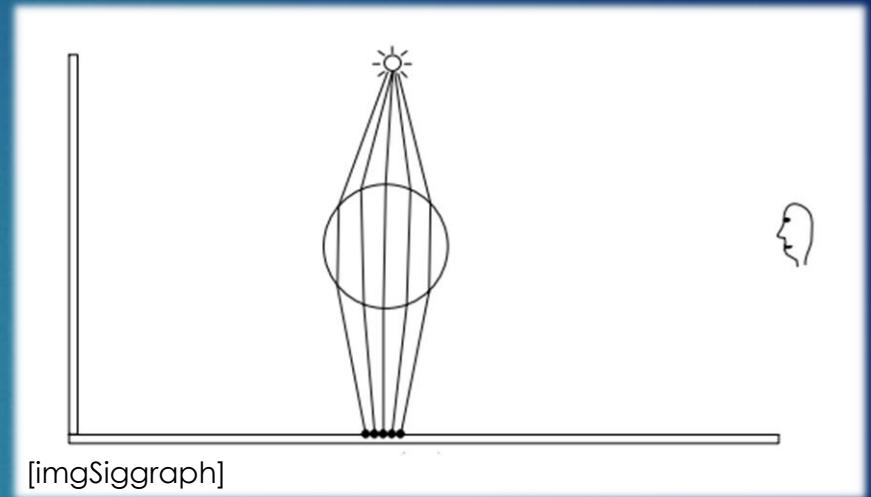
## Photon storing – KD-tree

- ▶ Photons are stored when they hit diffuse surfaces
- ▶ Use a KD-Tree
  - ▶  $O(\log N)$
  - ▶ Make sure is well balanced
    - ▶ Use an array to represent it

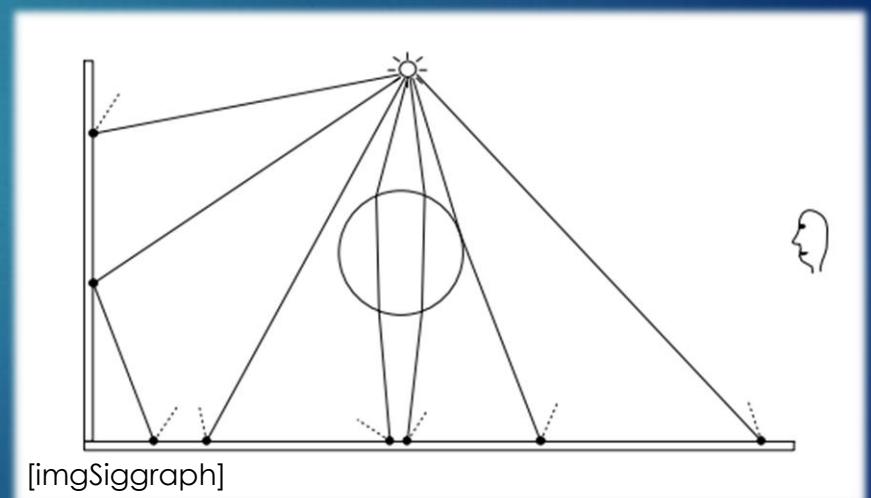
# Photon maps

Photon storing – Three maps

- ▶ Photon map types:
  - ▶ Caustics photon map → Caustics
    - ▶ Photon went at least through an specular reflection
  - ▶ Global photon map → Global illumination
    - ▶ Photons that hit a diffuse surface
  - ▶ Volume photon map → Indirect illumination
    - ▶ Indirect illumination of a participating medium



[imgSiggraph]



[imgSiggraph]

# Photon maps

## Summary

- ▶ Emit photons from all light sources
- ▶ Let the photons bounce through the scene
  - ▶ Use Russian roulette to determine action
    - ▶ Diffuse reflection, specular reflection or absorption
- ▶ Store the photons in the corresponding photon maps

# Rendering

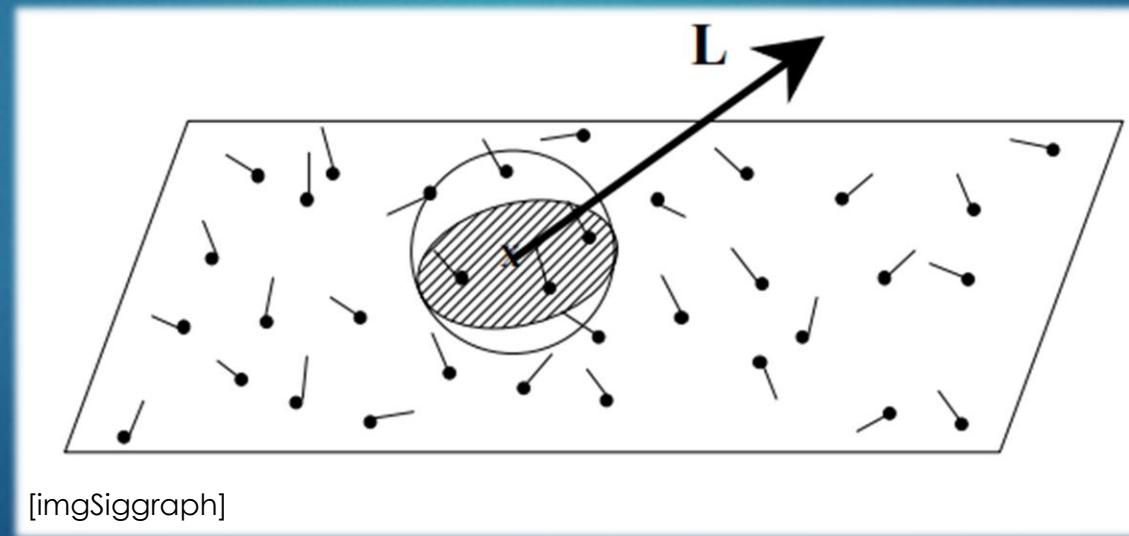


# Rendering

- ▶ Photon mapping is a 2 pass render technique
  1. Generate photon maps
  2. Use generated photon maps to get the radiance estimation on the surface

# Rendering

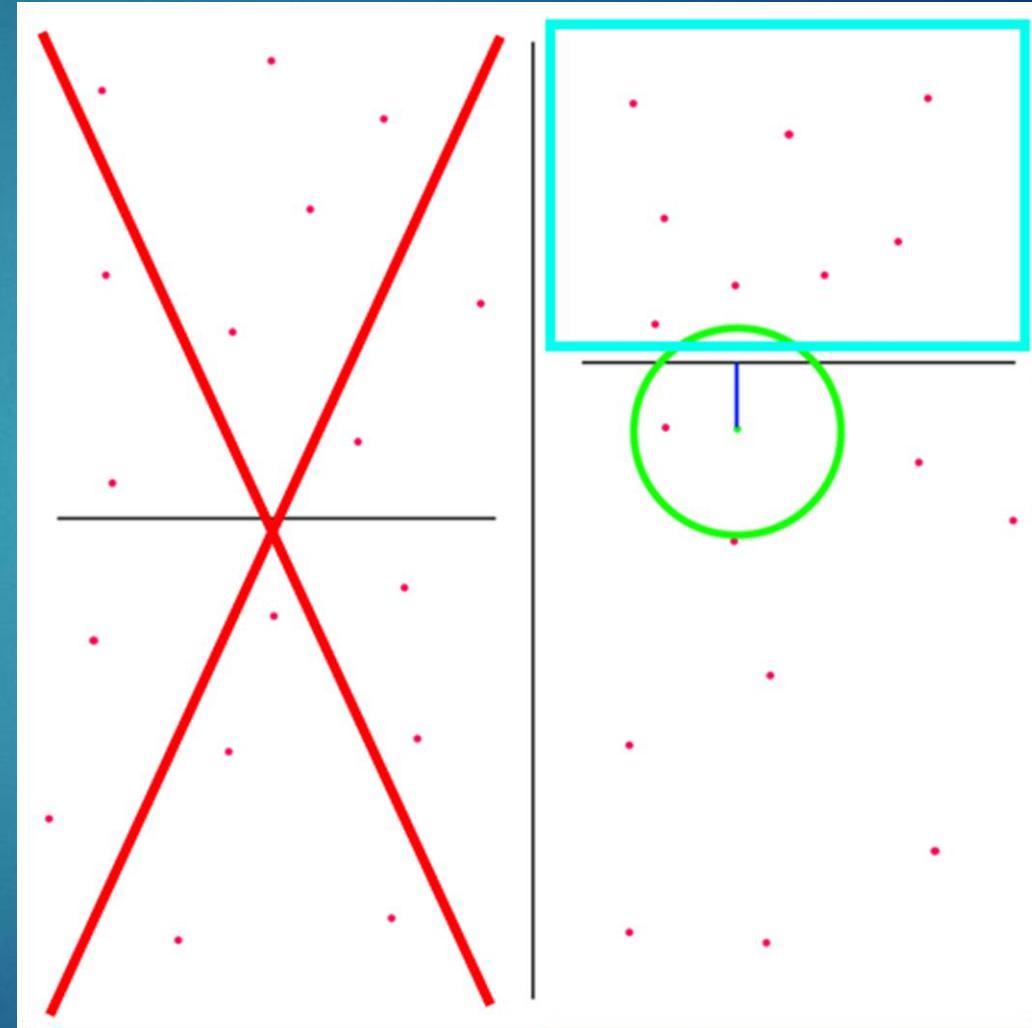
- ▶ Use the generated photon maps to get the radiance estimation
  - ▶ Caustics photon map
  - ▶ Global photon map
  - ▶ Volume photon map
- ▶ Get nearest photons in the surface → KD-Tree traversal



# Rendering

## KD-tree traversal

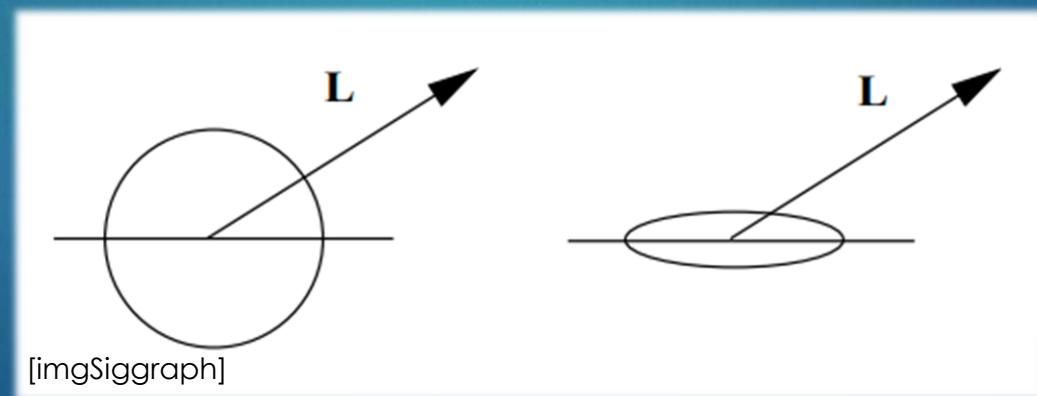
1. Check plane side
2. Traverse child node
3. Distance to plane < Threshold
1. Traverse other child



# Rendering

## Sphere VS Disk

- ▶ Sphere
  - ▶ Fast to locate photons, just need squared distance
  - ▶ Can give wrong approximations on corners
- ▶ Disk
  - ▶ Slower
  - ▶ More accurate, takes surface into account



# Rendering

## Radiance estimate – Formula

- ▶ Outgoing = Emitted + Reflected
  - ▶  $L_o$  → *Outgoing radiance*
  - ▶  $L_e$  → *Emitted radiance*
  - ▶  $L_r$  → *Reflected radiance*
  - ▶  $x$  → *Surface position*
  - ▶  $\vec{w}$  → *Direction (Surface to camera)*

$$L_o(x, \vec{w}) = L_e(x, \vec{w}) + L_r(x, \vec{w})$$

# Rendering

## Radiance estimate – Formula

- Reflected radiance is computed by integrating the incoming radiance
  - $f_r(x, \vec{w}', \vec{w}) \rightarrow$  Illumination function (in my case phong)
  - $L_i(x, \vec{w}')$  → Incoming radiance
  - $\Omega_x$  → hemi – sphere of incoming directions

$$L_r(x, \vec{w}) = \int_{\Omega_x} f_r(x, \vec{w}', \vec{w}) L_i(x, \vec{w}') |\vec{n}_x \cdot \vec{w}'| dw'_i$$

# Rendering

## Radiance estimate – Formula

- ▶ Apply relation between the radiance and the flux
- ▶ The flux is represented by photons in the photon map
  - ▶  $N \rightarrow$  number of photons near  $x$

$$L_r(x, \vec{w}) = \frac{1}{\pi r^2} \sum_{p=1}^N f_r(x, \vec{w}_p', \vec{w}) \Delta \Phi_p(x, \vec{w}_p)$$

# Rendering

## Radiance estimate – Formula

- ▶ Total incoming radiance  $L_i(x, \vec{w})$  is the sum of all radiances
  - ▶  $L_{i,l}(x, \vec{w}) \rightarrow$  Direct illumination
  - ▶  $L_{i,c}(x, \vec{w}) \rightarrow$  Caustics
  - ▶  $L_{i,d}(x, \vec{w}) \rightarrow$  Indirect illumination

$$L_i(x, \vec{w}) = L_{i,l}(x, \vec{w}) + L_{i,c}(x, \vec{w}) + L_{i,d}(x, \vec{w})$$

# Rendering

Radiance estimate – Formula

$$L_r(x, \vec{w}) = \int_{\Omega_x} f_r(x, \vec{w}', \vec{w}) L_i(x, \vec{w}') \ | \vec{n}_x \cdot \vec{w}' | \ dw'_i$$

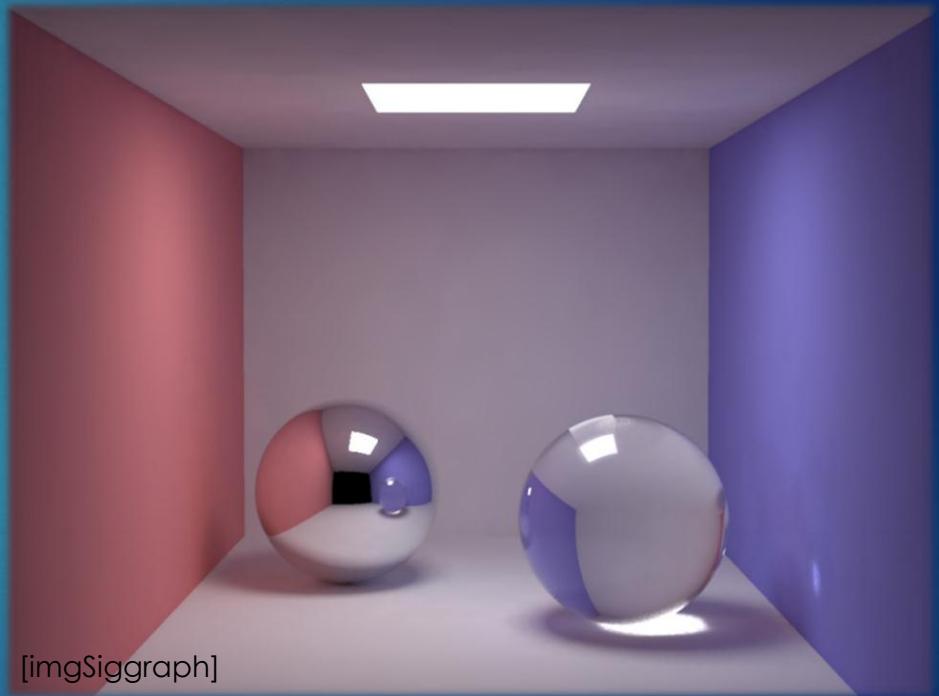
$$\frac{1}{\pi r^2} \sum_{p=1}^N f_r(x, \vec{w}_p', \vec{w}) \Delta \Phi_p(x, \vec{w}_p)$$

$$L_i(x, \vec{w}) = L_{i,l}(x, \vec{w}) + L_{i,c}(x, \vec{w}) + L_{i,d}(x, \vec{w})$$

# Rendering

## Radiance estimate - Filtering

- ▶ We average the flux in an area
- ▶ Special problem with Caustics
  - ▶ We want to preserve their sharp edges
- ▶ We use filtering to get better results
  - ▶ Increase weight of photons near the point of interest



[imgSiggraph]

# Rendering

## Radiance estimate - Filtering

- ▶ Gaussian filter
  - ▶  $d_p \rightarrow$  Distance from  $x$  to the photon
  - ▶  $\alpha = 0.918$
  - ▶  $\beta = 1.953$

$$w_{pg} = \alpha \left[ 1 - \frac{1 - e^{-\beta \frac{d_p^2}{2r^2}}}{1 - e^{-\beta}} \right]$$

$$L_r(x, \vec{w}) = \frac{1}{\pi r^2} \sum_{p=1}^N f_r(x, \vec{w_p}', \vec{w}) \Delta\Phi_p(x, \vec{w_p}) w_{pg}$$

# Summary



# Summary

- ▶ Photon mapping is a 2 pass rendering technique
  1. Generate photon maps
    - ▶ Use Russian roulette (reflect or absorb)
  2. Render scene
    - ▶ Use photon maps to get the radiance average
    - ▶ Apply filtering in case of caustics
      - ▶ Maintain sharp edges

# Conclusion



# Conclusion

## Why photon mapping?

- ▶ Photon mapping is less expensive than Monte Carlo integration
  - ▶ Russian roulette
    - ▶ Probabilistic approach to reduce the number of photons
  - ▶ Number of lights does not affect photon number
  - ▶ While rendering just need to find the nearest photons
    - ▶ KD-Tree →  $O(\log N)$

# Credits

- ▶ All the formulas and theoretical references of this presentation are from "Siggraph 2000 - A Practical Guide to Global Illumination using Photon Maps" (Order and arrangement of contents may not be the same)
  - ▶ <https://graphics.stanford.edu/courses/cs348b-00/course8.pdf>
- ▶ [imgSiggraph]: image taken from the document above
- ▶ [gif00]: Gif I created using giphy.com of the Bioshock Infinite game
  - ▶ <https://giphy.com/gifs/bioshock-infinite-zrqsuyczat4U8/>
- ▶ [gif01]: <https://opengameart.org/content/water-caustics-effect-small>
- ▶ [img00]: <https://commons.wikimedia.org/wiki/File:Caustics.jpg>
- ▶ [img01]: <https://www.flickr.com/photos/snogglethorpe/2612616268>
- ▶ [img02]: <http://therealrichard.deviantart.com/art/Caustics-and-Coloured-Emission-277601210>



# Thanks for listening!

## Questions?